

# A Century of Evidence on Trend-Following Investing

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is a principal at AQR Capital Management in Greenwich, CT, and a professor at Copenhagen Business School in Frederiksberg, Denmark, and New York University in New York, NY. s an investment style, trend following has existed for a very long time. Some 200 years ago, the classical economist David Ricardo's imperative to "cut short your losses" and "let your profits run on" suggests an attention to trends. A century later, the legendary trader Jesse Livermore stated explicitly that the "big money was not in the individual fluctuations but in…sizing up the entire market and its trend."<sup>1</sup>

The most basic trend-following strategy is time-series momentum—going long markets with recent positive returns and shorting those with recent negative returns. The literature shows that since 1985, timeseries momentum has been profitable, on average, for nearly all equity index futures, fixed-income futures, commodity futures, and currency forwards.<sup>2</sup> The strategy explains the strong performance of managed futures funds from the late 1980s, when fund returns and index data first become available,<sup>3</sup> and captures most forms of trend-following investing.<sup>4</sup>

In this article, we seek to establish whether the strong performance of trend following is a statistical fluke of the last few decades or a more robust phenomenon that exists over a wide range of economic conditions. We construct a time-series momentum strategy all the way back to 1880 using historical data from a number of sources, including novel data on commodity futures prices that we hand collect and transcribe from annual reports of the Chicago Board of Trade.<sup>5</sup>

We find that time-series momentum has been consistently profitable throughout the past 137 years. We examine the strategy's decade-by-decade performance, its correlation to major asset classes, and its performance in historical equity bull and bear markets. This wealth of data also provides context for evaluating how the strategy performs across various macroeconomic environmentssuch as recessions versus booms, war versus peacetime, high- versus low-interest-rate regimes, high- versus low-volatility periods, high-versus low-inflation periods, and highversus low-correlation periods. Although the strategy has historically performed well across most of these economic environments, the characteristic that appears to have affected the performance the most is correlation-the strategy has performed the best during lowcorrelation environments. We also estimate the effects of fees and transaction costs and evaluate the benefits of allocating to a trendfollowing strategy from a traditional stock/ bond portfolio.

#### DATA

In our analysis, we use monthly returns for 67 markets across four major asset classes: 29 commodities, 11 equity indices, 15 bond markets, and 12 currency pairs. To study the broadest set of markets over the longest time series in which we can find data, we combine a large number of existing datasets and hand collect new data that have not been studied previously, to our knowledge. In particular, we construct a novel dataset of daily commodities futures prices by manually transcribing the "Annual Report of the Trade and Commerce of the Chicago Board of Trade" going back as early as 1877. The hand-collected data extends to 1951, when electronic datasets became available. For the study, we use a monthly sample based on end-of-month prices and returns.

We construct a monthly time series of futures returns by simulating that we hold, and "roll," one of the most liquid futures contracts. In particular, we "roll" by simultaneously performing two trades: (1) selling the futures contract that we held and (2) buying the next futures contract, while collecting the current prices of *both* contracts to make the analysis as realistic as possible. We focus on closing prices when available, but in the early sample of commodities, we only have access to high and low prices; thus, we use an average of these.

For all markets, we use futures returns when they are available, but for asset classes other than commodities, futures are not available back to 1877. Hence, prior to the availability of futures data, we rely on cash index returns financed at local short-term interest rates for each country. Our time-series momentum strategy requires three years of past data to estimate volatilities, so our sample of simulated strategy returns runs from 1880 to the end of 2016. We do not have data on each of the 67 markets during each month in this sample, so we construct the trend-following strategies using the set of assets for which return data exist at each point in time. Appendix A shows the markets for which we have data at each point in time and the respective data sources for each market and each time period.<sup>6</sup>

### CONSTRUCTING THE TIME-SERIES MOMENTUM STRATEGY

Trend-following investing involves going long markets that have been rising and going short markets that have been falling, betting that those trends continue. We create a time-series momentum strategy that is simple, without many of the often arbitrary choices of more complex models. Our methodology follows that of Moskowitz et al. [2012] and Hurst et al. [2013] and can thus be viewed as an out-of-sample test of those papers. These studies find that time-series momentum captures well the performance of the managed futures indices and manager returns, including the largest funds, over the past few decades when data on such funds exist.

Specifically, we construct an equal-weighted combination of 1-month, 3-month, and 12-month timeseries momentum strategies for the 67 markets cited above—from as far back as January 1880 to December 2016. The strategy is rebalanced each month as follows. For each of the three time-series momentum strategies, the position taken in each market is determined by assessing the past excess return in that market over the relevant look-back horizon. A positive past excess return is considered an "up" trend and leads to a long position; a negative past excess return is considered a "down" trend and leads to a short position.

Therefore, each strategy always holds either a long or short position in every market. Each position is sized to target the same amount of volatility, both to provide diversification and to limit the portfolio risk from any one market. The positions across the three strategies are aggregated each month and scaled such that the combined portfolio has an annualized ex ante volatility target of 10% annualized.<sup>7</sup> The volatility scaling procedure ensures that the combined strategy targets a consistent amount of risk over time, regardless of the number of markets traded at each point in time.

Finally, we subtract transaction costs and fees. The transaction costs are based on recent estimates of average transaction costs in each of the four asset classes, as well as an estimate of how much higher these transaction costs were historically, based on Jones [2002]. We note that transaction costs are estimated with a significant amount of uncertainty, and the strategy may also be subject to other costs such as the costs of "rolling" futures contracts, which are not accounted for in our simulations. To simulate fees, we apply a 2% management fee and a 20% performance fee subject to a highwater mark, as has been typical for hedge funds.<sup>8</sup> Details on transaction costs and fee simulations are given in Appendix B.

#### PERFORMANCE OVER A CENTURY

Exhibit 1 shows the performance of the time-series momentum strategy over the full sample since 1880, as well as for each decade over this time period. We report

Time Period	Gross of Fee, Gross of Cost Excess Returns	Gross of Fee, Net of Cost Excess Returns	Net of 2/20 Fee, Net of Cost Excess Returns	Realized Volatility	Sharpe Ratio, Net of Fees and Costs	Correlation to U.S. Equity Market	Correlation to U.S. 10-Year Bond Returns
Full Sample							
Jan 1880–Dec 2016	18.0%	11.0%	7.3%	9.7%	0.76	-0.01	-0.03
By Decade							
Jan 1880–Dec 1889	12.1%	5.2%	2.6%	9.5%	0.27	-0.11	-0.04
Jan 1890–Dec 1899	17.4%	10.0%	6.5%	8.9%	0.73	-0.02	-0.15
Jan 1900–Dec 1909	15.3%	6.0%	3.3%	9.5%	0.34	0.02	-0.35
Jan 1910–Dec 1919	12.5%	4.1%	1.6%	12.6%	0.13	0.12	-0.01
Jan 1920–Dec 1929	20.8%	13.3%	9.2%	8.5%	1.09	0.15	0.06
Jan 1930–Dec 1939	15.4%	9.8%	6.3%	8.6%	0.74	-0.11	0.20
Jan 1940–Dec 1949	23.8%	14.8%	10.4%	10.6%	0.99	0.33	0.31
Jan 1950–Dec 1959	26.7%	17.6%	13.1%	9.1%	1.45	0.23	-0.19
Jan 1960–Dec 1969	21.0%	9.5%	6.0%	10.9%	0.56	-0.09	-0.37
Jan 1970–Dec 1979	27.4%	20.5%	15.1%	8.9%	1.70	-0.24	-0.25
Jan 1980–Dec 1989	20.1%	13.3%	9.1%	9.4%	0.96	0.18	-0.16
Jan 1990–Dec 1999	16.8%	12.3%	8.3%	8.4%	0.98	0.01	0.21
Jan 2000–Dec 2009	11.6%	9.9%	6.3%	10.3%	0.61	-0.34	0.27
Jan 2010–Dec 2016	7.6%	6.2%	3.3%	8.1%	0.41	-0.15	0.28

# Performance of Time-Series Momentum, 1880–2016

Note: This exhibit shows the strategy's annualized excess returns (i.e., returns in excess of the risk-free interest rate), before and after simulated transaction costs, and gross and net of hypothetical 2-and-20 fees.

the results gross and net of simulated transaction costs and consider returns both before and after fees.

The performance has been surprisingly consistent over an extensive time horizon that includes the Great Depression, multiple recessions and expansions, multiple wars, stagflation, the global financial crisis, and periods of rising and falling interest rates. Our long-term out-of-sample evidence suggests that it is unlikely that the existence of price trends in markets is a product of statistical randomness or data mining. Indeed, the first 10 decades of data is out-of-sample evidence relative to the literature, and the performance remains strong during this period. Trends thus appear to be a pervasive characteristic of speculative financial markets over the long term.

Time-series momentum strategies perform well only if prices trend more often than not. A large body of research suggests that price trends exist in part because of long-standing behavioral biases exhibited by investors,<sup>9</sup> such as anchoring and herding, as well as the trading activity of nonprofit-seeking participants, such as central banks and corporate hedging programs. For instance, when central banks intervene to reduce currency and interest rate volatility, they may slow down the rate at which information is incorporated into prices, thus creating trends. The fact that trend-following strategies have performed well historically indicates that these behavioral biases and nonprofit-seeking market participants have likely existed for a long time.

To study the robustness and source of these results, Exhibit 2 considers the performance separately for the 1-month, 3-month, and 12-month signals. We see that trend-following at each of these horizons has delivered positive returns in each decade. To further study the robustness and ability to implement these strategies, we consider a version in which the signal is lagged a month. In other words, if the trend signal is computed at the last trading day of January, we assume that we trade on this signal only at the end of February (in the same year). As seen in Exhibit 2, these strategies also deliver positive returns in most decades, but the performance naturally deteriorates with the lagging, especially for the shorter-term signals.

Given the consistent performance of the strategy over time, it is also interesting to study the consistency across markets. For this, Exhibit 3 reports the

# **E** X H I B I T **2** Performance of Time-Series Momentum by Signal

Time Period	1-Month Strategy	1-Month Strategy (lagged)	3-Month Strategy	3-Month Strategy (lagged)	12-Month Strategy	12-Month Strategy (lagged)
Full Sample						
Jan 1880–Dec 2016	1.38	0.45	1.19	0.64	1.32	1.04
By Decade						
Jan 1880–Dec 1889	1.02	-0.34	0.78	-0.23	1.03	0.89
Jan 1890–Dec 1899	1.32	0.34	0.91	0.25	1.35	0.83
Jan 1900–Dec 1909	0.87	0.35	1.20	0.65	1.52	1.52
Jan 1910–Dec 1919	0.80	0.01	0.63	0.39	0.99	0.83
Jan 1920–Dec 1929	1.75	0.56	1.23	0.51	1.77	1.27
Jan 1930–Dec 1939	1.19	0.27	1.21	0.29	1.09	0.70
Jan 1940–Dec 1949	2.16	1.09	1.65	1.29	1.54	1.27
Jan 1950–Dec 1959	2.48	1.48	1.95	1.38	1.55	1.27
Jan 1960–Dec 1969	1.81	0.31	1.31	0.68	1.01	0.42
Jan 1970–Dec 1979	2.24	0.82	2.13	1.34	1.91	1.66
Jan 1980–Dec 1989	1.77	0.40	1.09	0.50	1.46	1.07
Jan 1990–Dec 1999	1.13	0.49	1.52	0.75	1.38	1.20
Jan 2000–Dec 2009	0.70	0.38	0.67	0.66	1.10	0.86
Jan 2010–Dec 2016	0.06	0.13	0.30	0.33	0.73	0.70

Notes: This exhibit shows the annualized gross Sharpe ratio (i.e., excess return before simulated transaction costs and fees divided by volatility) separately for each time-series momentum signal based on the past 1-month, 3-month, and 12-month trend, respectively. Also, the table shows the performance when each of these signals is lagged by one month.

risk-adjusted returns (as measured by the Sharpe ratio) of each of the 67 markets included in our time-series momentum strategy over the full sample from 1880 to 2016. We see that the strategy has delivered positive average returns in each market, with an average Sharpe ratio of approximately 0.4.

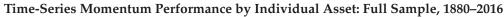
We next consider the out-of-sample evidence for individual markets relative to the initial time-series momentum study of Moskowitz et al. [2012], who used data starting in 1985. To do this, we report the performance of each market before 1985 in Exhibit 4, including only markets with at least 10 years of data during this subsample, 1880–1984. Again, we see a remarkably consistent performance across markets and asset classes.

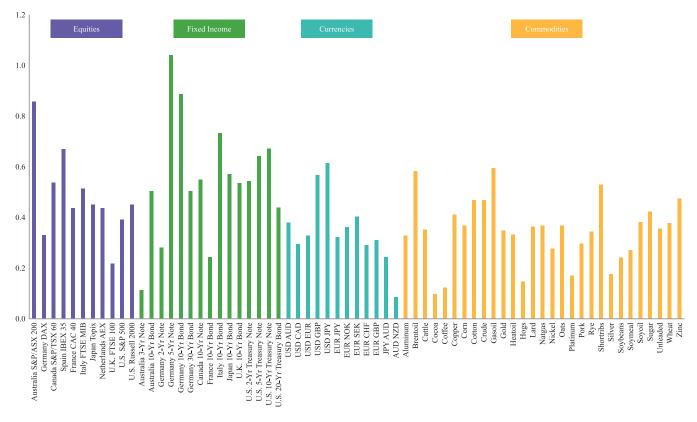
## PERFORMANCE DURING CRISIS PERIODS

The returns to the strategy have exhibited low correlations to stocks and bonds over the full time period, as well as in each decade, as shown in Exhibit 1. Even more impressively, the strategy has performed best in large equity bull and bear markets. Exhibit 5 shows the annual simulated returns to the strategy, plotted against the returns to the U.S. equity market from 1880 to 2016. The "smile" shows that trend following has done particularly well in extreme up or down years for the stock market, echoing results from recent decades (Fung and Hsieh [1997] and Moskowitz et al. [2012]). This strong performance in bear markets over the century extends the evidence that has been documented since the 1980s, as exemplified most recently with the strong performance of trend following during the global financial crisis.

As another way to evaluate the diversifying properties of trend following during crisis periods, we consider the performance during peak-to-trough drawdowns for the traditional 60/40 portfolio, which invests 60% in U.S. equities and 40% in U.S. bonds.<sup>10</sup> Exhibit 6 shows the performance of the time-series momentum strategy during the 10 largest drawdowns experienced by this 60/40 portfolio over the past 137 years. We see that the time-series momentum strategy experienced positive returns in 8 out of 10 of these stress periods and

EXHIBIT 3





Note: This exhibit shows the Sharpe ratio of time-series momentum (gross of fee, gross of cost) by asset.

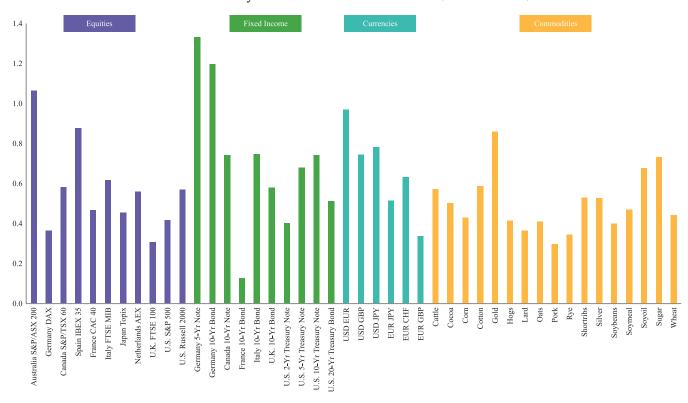
delivered significant positive returns during a number of these events. Hence, the valuable diversification benefits that trend-following strategies delivered during the 2007–2009 Global Financial Crisis may represent a more general pattern when you consider how the strategy has behaved in other deep bear markets over the century.

Why have trend-following strategies tended to do well in bear markets? The intuition is that most bear markets have historically occurred gradually over several months, rather than abruptly over a few days, giving trend followers an opportunity to position themselves short after the initial market decline and profit from continued market declines. In fact, the average peakto-trough drawdown length of the 10 largest 60/40 drawdowns between 1880 and 2016 was approximately 15 months. In contrast, the strategy may not perform well in bear markets that occur very rapidly, such as the 1987 stock market crash, because the strategy may not be able to take positions quickly enough to benefit from sharp market movements in those environments. Nevertheless, the tendency for the strategy to do well, on average, in major bear markets, while still achieving a positive return, on average, makes it a potentially valuable diversifier for investor portfolios.

Given the attractive returns and diversifying characteristics of a time-series momentum strategy, allocating to this strategy would have improved a traditional portfolio's performance over the past 137 years. Specifically, Exhibit 7 shows the simulated effect of allocating 20% of the capital from a 60/40 portfolio to the time-series momentum strategy. We see that such an allocation reduced the maximum portfolio drawdown, lowered portfolio volatility, and increased portfolio returns.

We can also consider the stress periods for timeseries momentum (rather than the stress periods for the overall market), which tend to be associated with periods of sharp reversals across multiple markets or

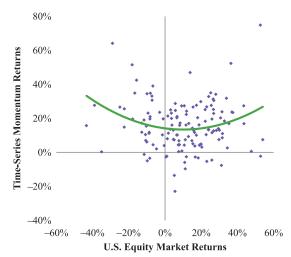
Ехнівіт 4



Time-Series Momentum Performance by Individual Asset: Before 1985 (new evidence)

Notes: This exhibit shows the Sharpe ratio of time-series momentum (gross of fee, gross of cost) by asset, 1880–1984. We include only assets that have at least 10 years of data before 1985. This evidence is out of sample relative to the study of Moskowitz et al. [2012].

# E X H I B I T 5 Time-Series Momentum "Smile," 1880–2016

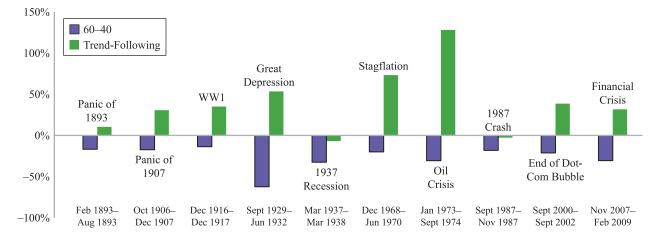


Note: This exhibit shows the annual returns of time-series momentum (gross of fee, net of cost) vs. U.S. equity market returns, as well as the fitted second-order polynomial.

prolonged periods in which many markets exhibit a lack of clear trends. Specifically, Exhibit 8 shows the 10 largest drawdowns of the time-series momentum strategy, including the amount of time the strategy took to realize and recover from each drawdown. The drawdown is computed as the percentage loss since the strategy reached its highest-ever cumulative return (its high-water mark). Naturally, the strategy has experienced significant drawdowns, losing up to 25%, over extended time periods.

# PERFORMANCE ACROSS ECONOMIC ENVIRONMENTS

We next consider the performance across different economic environments. This is interesting both to understand the nature of the strategy and to further analyze its potential diversification benefits. Indeed, investors benefit most from strategies that deliver high returns during



#### Time-Series Momentum during the 10 Worst Drawdowns for 60/40

Note: This exhibit shows the returns of time-series momentum (gross of fee, net of cost) and return of the portfolio that invested 60% in U.S. stocks and 40% in U.S. bonds over the 10 time periods selected as the largest drawdowns for the latter portfolio.

# E X H I B I T 7 Combining 60/40 with an Allocation to Time-Series Momentum, January 1880 to December 2016

	Annualized Excess of Cash Returns	Annualized Vol	Max Drawdown	Net of Fee Sharpe Ratio
60/40 Portfolio	4.1%	10.7%	-62.3%	0.39
80% 60/40 Portfolio,	4.8%	8.7%	-50.2%	0.55
20% Time-Series				
Momentum Strategy				

Notes: This exhibit reports the historical performance characteristics of the 60/40 portfolio that invested 60% in U.S. equities and 40% in U.S. bonds. Also, the table reports the performance of a portfolio with 80% invested in the 60/40 portfolio (gross of fees and transaction costs) and 20% invested in the time-series momentum strategy (net of fees and transaction costs).

"tough times" when their marginal utility of wealth is high. We have already considered the performance during crisis periods as defined by drawdowns by 60/40, but several other economic environments are of interest.

Exhibit 9, Panel A, considers the performance of time-series momentum across different regimes, starting with the two classic macroeconomic characteristics (or themes), growth and inflation. To analyze macroeconomic growth, we separate the months into recessions and booms as defined by the NBER Business Cycle Dating Committee. We see that the performance is similar across these environments. The average excess return has been slightly higher during booms, but the difference is not statistically significant. Next, the exhibit reports the performance across low- versus high-inflation environments, and, again we find very similar performance for timeseries momentum. The strong performance during recessions and different inflation regimes is evidence of the historical diversifying properties of the strategy.

It is also interesting to consider the performance during "tough times" in the sense of wartime. There have been so many conflicts around the world that defining wartime and peacetime is not straightforward. To have a clear-cut definition, we focus on the largest wars defined as those with more than 1 million casualties with at least three nations at war—which are World War 1, World War 2, the Vietnam War, and the Korean War, with "peace" being all other time periods (again, despite the numerous other conflicts). We see that the strategy has performed similarly across both samples. If anything,

EXHIBIT 8
The 10 Largest Drawdowns of Time-Series Momentum, 1880–2016

Rank	Start of Drawdown (peak)	Lowest Point of Drawdown (trough)	End of Drawdown (recovery)	Size of Peak- to-Trough Drawdown	Excess Return During Peak- to-Trough Drawdown	Peak-to- Trough Length (months)	Trough-to- Recovery Length (months)
1	Aug 1947	Dec 1948	Feb 1951	-24.7%	-26.1%	16	26
2	Apr 1912	Jan 1913	Aug 1914	-22.8%	-26.3%	9	19
3	Feb 1937	Jun 1940	Aug 1941	-21.2%	-21.6%	40	14
4	Mar 1918	Feb 1919	Feb 1920	-20.4%	-25.6%	11	12
5	Aug 1966	Dec 1966	Mar 1968	-17.7%	-19.4%	4	15
6	Jun 1964	Aug 1965	Dec 1965	-17.2%	-21.6%	14	4
7	Mar 2015	May 2016	N/A	-16.1%	-16.2%	14	N/A
8	Aug 1896	Jun 1897	Dec 1898	-15.0%	-17.7%	10	18
9	Apr 1885	Jun 1885	Jul 1887	-14.4%	-14.6%	2	25
10	Feb 1904	Jul 1904	Jun 1906	-14.1%	-15.1%	5	23

Note: This exhibit reports the 10 largest peak-to-trough drawdowns of the time-series momentum strategy, calculated using gross of fee, net of cost returns.

the performance has been better during major wars, but the difference is not statistically significant.

Lastly, the table in Exhibit 9, Panel B, considers bull markets versus bear markets; bear markets are defined as periods in which the peak-to-trough drawdown of the U.S. equity market is greater than 20%, and bull markets are all other times. The strategy has performed better in bear markets, but the difference is only marginally significant, and perhaps the more robust result is the smile curve in Exhibit 5.

Exhibit 9, Panel B, considers the same economic environments, but now the economic environment is lagged by one month. For example, this panel considers the performance of trend-following investing during the month after a recession month (so the month in which the return is calculated might, or might not, continue to be a recession).

Panels A and B thus address different issues: Panel A takes the perspective of an investor who stands at the *end* of each month, looking back at the performance of trend following in relation to the economic environment experienced during the same month. This perspective cannot be used to make timing decisions in the portfolio because the economic environment was not known ahead of time. In contrast, Panel B takes the perspective of an investor who stands at the *beginning* of each month, looking at the performance of trend following in the coming month in relation to the economic environment experience in the previous month. Such a prospective analysis could be used to time a trading strategy, in principle, but we note several caveats. First, certain variables are not known in real time (e.g., the dating of recessions), and second, the classification of low versus high inflation is performed ex post. In any event, Panel B shows that the performance of trend following was similar across groups. Hence, whereas Panel B shows the apparent difficulty of improving the strategy via timing decisions, Panel A shows the good news that the strategy appears to be relatively robust across various economic environments.

In Exhibit 10, we consider different economic indicators, while separating the time periods into quintiles (because each of these indicators are numerical, rather than binary variables such as war/peace or recession/boom). In particular, we consider the S&P volatility (estimated over the most recent 36 months), the 3-month change in the estimated volatility, the average absolute pairwise correlations across the markets traded in the portfolio, and the T-bill yield. Panel A reports the contemporaneous time-series momentum performance, while Panel B reports the performance in the following month (or, said differently, the economic indicator is lagged one month, as in Exhibit 9, Panel B).

Starting with the first row of Exhibit 10, Panel A, we see that time-series momentum has performed best in quintiles 3 and 2, where the contemporaneous S&P 500 volatility was average or just below average, although this result could also simply reflect randomness in the data.

Panel A: Time- Macro Indicato	Macro Indicators					Panel B: Time-Series Momentum Returns by Lagged Macro Indicators					
Macro Indicator	Statistic	Group 1	Group 2	Difference	Macro Indicator	Statistic	Group 1	Group 2	Difference		
Recession	Excess return	10.4%	11.2%	0.8%	Recession	Excess return	10.1%	11.4%	1.3%		
vs. Boom	(t-statistic)	(5.4)	(10.7)	(0.4)	vs. Boom	(t-statistic)	(5.1)	(11.0)	(0.6)		
	Volatility	11.6%	10.5%			Volatility	11.9%	10.4%			
	Sharpe ratio	0.90	1.07			Sharpe ratio	0.84	1.09			
	% of occurrences	26%	74%			% of occurrences	26%	74%			
Inflation:	Excess return	10.5%	11.5%	1.0%	Inflation:	Excess return	11.8%	10.2%	-1.7%		
Low vs. High	(t-statistic)	(8.4)	(8.4)	(0.5)	Low vs. High	(t-statistic)	(9.7)	(7.3)	(-0.9)		
	Volatility	10.5%	11.2%			Volatility	10.3%	11.4%			
	Sharpe ratio	1.01	1.03			Sharpe ratio	1.15	0.90			
	% of occurrences	51%	49%			% of occurrences	51%	49%			
War vs. Peace	Excess return	13.5%	10.2%	-3.3%	War vs. Peace	Excess return	13.8%	10.1%	-3.7%		
	(t-statistic)	(6.7)	(9.9)	(-1.5)		(t-statistic)	(6.8)	(9.8)	(-1.6)		
	Volatility	11.5%	10.6%			Volatility	11.6%	10.5%			
	Sharpe ratio	1.17	0.97			Sharpe ratio	1.19	0.96			
	% of occurrences	24%	76%			% of occurrences	24%	76%			
Stock Market:	Excess return	10.2%	15.5%	5.3%	Stock Market:	Excess return	10.3%	14.8%	4.5%		
Bull vs. Bear	(t-statistic)	(10.4)	(5.9)	(1.9)	Bull vs. Bear	(t-statistic)	(10.6)	(5.6)	(1.6)		
	Volatility	10.6%	12.0%			Volatility	10.6%	12.1%			
	Sharpe ratio	0.96	1.30			Sharpe ratio	0.98	1.22			
	% of occurrences	85%	15%			% of occurrences	85%	15%			

Time-Series Momentum across Economic Regimes: Binary Indicators

Notes: This exhibit shows the performance of the time-series momentum strategy before fees and after simulated transaction costs. For each economic regime, we report the strategy's annualized excess return, its t-statistic, volatility, and Sharpe ratio. The regimes are "recession vs. boom" indicators as defined by NBER Business Cycle Dating Committee; "inflation: low vs. high" based on U.S. CPI from 1913 to 2016 and before 1913, based on Shiller [2000] who uses the Warren and Pearson [1935] price index; "war vs. peace," where war periods are World War 1, World War 2, the Vietnam War, and the Korean War and peace are other time periods; "stock market: bull vs. bear," where bear markets are defined as periods where peak to trough drawdown of U.S. equity market is greater than 20% and bull market is all other times. In Panel A, we consider the contemporaneous effect—for example, for "war," we compute the return during each recession month of war even if the war started midmonth. In Panel B, we lag the indicator of the economic environment—for example, for "war," we compute the return each month following a war month.

Further, the performance has been similar across quintiles based on changes in equity market volatility and the level of Treasury bill yields. While some practitioners have described trend following as a strategy that is "long volatility," the quintile sorts on changes in equity volatility show that the strategy's performance has historically been relatively consistent across periods of increasing and decreasing market volatility. Looking at the pairwise correlations across markets, we see that lower correlations appear to have been associated with better performance.

Turning to Panel B, we see a similar pattern, which could be related to the persistence of the economic indicators. Again, the only indicator with a monotonic relation to the performance of time-series momentum is the pairwise correlation across markets. We see that low lagged correlations are associated with higher average future returns, while high correlations are associated with low returns. To understand this finding, note first that for given notional exposures, a higher correlation implies a higher risk at the portfolio level. However, because our portfolio construction methodology seeks to target a constant volatility, this effect is "undone" by reducing all position sizes when correlations are high. These lower position sizes in turn may lead to lower average returns, which can help explain why the strategy performs worse during times of high correlations. Said differently, when correlations are high, there are fewer truly different trends to bet on.

Exhibit 11 plots the time series of the average absolute pairwise correlation across all the markets used in

Macro Indicator	Statistic	Quintile 1	Quintile 2	Quintile 3	Quintile 4	Quintile !
Panel A: Time-Series Mo	mentum Returns by	v Contemporaneo	ous Macro Indica	itors		
S&P Volatility Level	Excess return	6.9%	15.8%	15.9%	8.5%	8.0%
(Horizon: 36 Months)	(t-statistic)	(3.0)	(7.7)	(8.2)	(4.2)	(4.1)
	Volatility	11.9%	10.8%	10.2%	10.6%	10.2%
	Sharpe ratio	0.58	1.46	1.56	0.80	0.78
S&P Volatility Change	Excess return	13.1%	10.6%	10.1%	10.6%	10.7%
(Horizon: 3 Months)	(t-statistic)	(6.9)	(5.2)	(5.3)	(5.3)	(4.3)
	Volatility	9.9%	10.6%	10.0%	10.3%	13.0%
	Sharpe ratio	1.32	1.00	1.01	1.02	0.83
Absolute Pairwise	Excess return	17.1%	15.0%	8.6%	6.3%	8.0%
Correlation	( <i>t</i> -statistic)	(8.1)	(7.4)	(4.3)	(3.4)	(3.5)
	Volatility	11.1%	10.6%	10.5%	9.6%	11.9%
	Sharpe ratio	1.54	1.42	0.83	0.66	0.67
T-Bill Yields	Excess return	12.2%	10.2%	7.5%	11.9%	13.2%
	(t-statistic)	(5.8)	(4.9)	(4.1)	(5.8)	(5.9)
	Volatility	11.1%	10.9%	9.4%	10.8%	11.7%
	Sharpe ratio	1.10	0.94	0.79	1.10	1.13
Panel B: Time-Series Mo	mentum Returns by	v Lagged Macro	Indicators			
S&P Volatility Level	Excess return	7.8%	15.9%	15.2%	6.4%	9.8%
(Horizon: 36 Months)	( <i>t</i> -statistic)	(3.4)	(7.5)	(7.7)	(3.2)	(5.3)
· · · · · · · · · · · · · · · · · · ·	Volatility	12.0%	11.2%	10.3%	10.5%	9.7%
	Sharpe ratio	0.65	1.43	1.47	0.61	1.00
S&P Volatility Change	Excess return	14.1%	10.3%	7.9%	12.1%	10.6%
(Horizon: 3 Months)	( <i>t</i> -statistic)	(7.3)	(5.1)	(3.8)	(5.8)	(4.8)
	Volatility	10.1%	10.6%	10.8%	10.9%	11.6%
	Sharpe ratio	1.40	0.98	0.73	1.11	0.91
Absolute Pairwise	Excess return	18.8%	14.1%	8.7%	7.3%	6.2%
Correlation	(t-statistic)	(8.4)	(6.8)	(4.9)	(3.6)	(3.0)
	Volatility	11.7%	10.9%	9.4%	10.6%	11.0%
	Sharpe ratio	1.61	1.29	0.93	0.69	0.57
T-Bill Yields	Excess return	11.1%	11.8%	8.7%	10.3%	13.2%
	( <i>t</i> -statistic)	(5.5)	(5.9)	(4.4)	(5.0)	(5.9)
	Volatility	10.7%	10.5%	10.4%	10.7%	11.7%
	Sharpe ratio	1.04	1.12	0.84	0.96	1.13

## **Time-Series Momentum across Economic Regimes: Quintiles**

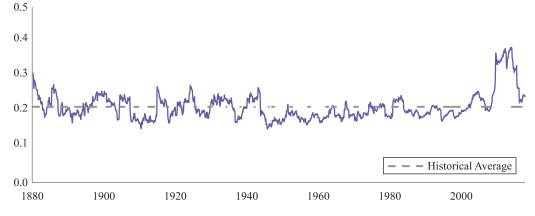
Notes: This exhibit shows the performance of the time-series momentum strategy before fees and after simulated transaction costs. For each economic regime, we report the strategy's annualized excess return, its t-statistic, volatility, and Sharpe ratio. We consider the economic indicators: S&P volatility (estimated over the most recent 36 months), the 3-month change in the estimated volatility, the average absolute pairwise correlations across the markets, and the T-bill yield. For each indicator, we sort the data into quintiles. Panel A reports the contemporaneous time-series momentum performance, and Panel B reports the time-series momentum performance in the following month.

our strategy. We see that the average correlations have been relatively stable over time, but increased meaningfully from late 2008 until the middle of 2014. During this period, the many markets moved together based on "risk-on/risk-off," leading to higher correlations both within and across asset classes.

#### CONCLUSION

Trend-following investing has performed well in each decade for more than a century, as far back as we can get reliable return data for several markets. Our analysis provides significant out-of-sample evidence across markets and asset classes beyond the substantial

**E** X H I B I T **11** Average Absolute Pairwise Asset Correlations



Note: This exhibit shows the absolute pairwise correlations across all assets available at each time, estimated over 36 months.

evidence already in the literature. Further, we find that a trend-following strategy performed relatively similarly across a variety of economic environments and provided significant diversification benefits to a traditional allocation. This consistent long-term evidence suggests that trends are pervasive features of global markets.

# APPENDIX A

# MARKETS AND DATA SOURCES

We use historical return data from 67 markets, as seen in Exhibit A1. Our data sources are as follows:

**Equity indices.** The universe of equity index futures consists of the following 11 developed equity markets: SPI 200 (Australia), S&P/TSE 60 (Canada), CAC 40 (France), DAX (Germany), FTSE/MIB (Italy), TOPIX (Japan), AEX (Netherlands), IBEX 35 (Spain), FTSE 100 (U.K.), Russell 2000 (U.S.) and S&P 500 (U.S.). Futures returns are obtained from Datastream and Bloomberg. We use MSCI country-level index returns and returns from Ibbotson, Global Financial Data (GFD), and the Yale School of Management prior to the availability of futures returns.

**Bond indices.** The universe of bond index futures consists of the following 15 developed bond markets: Australia 3-year bond, Australia 10-year bond, Euro Schatz (2-year), Euro Bobl (5-year), Euro Bund (10-year), Euro Buxl (30-year), Canada 10-year bond, Japan 10-year bond (TSE), long gilt, U.S. 2-year note, Italian 10-year bond, French 10-year bond, U.S. 5-year note, U.S. 10-year note, and U.S.

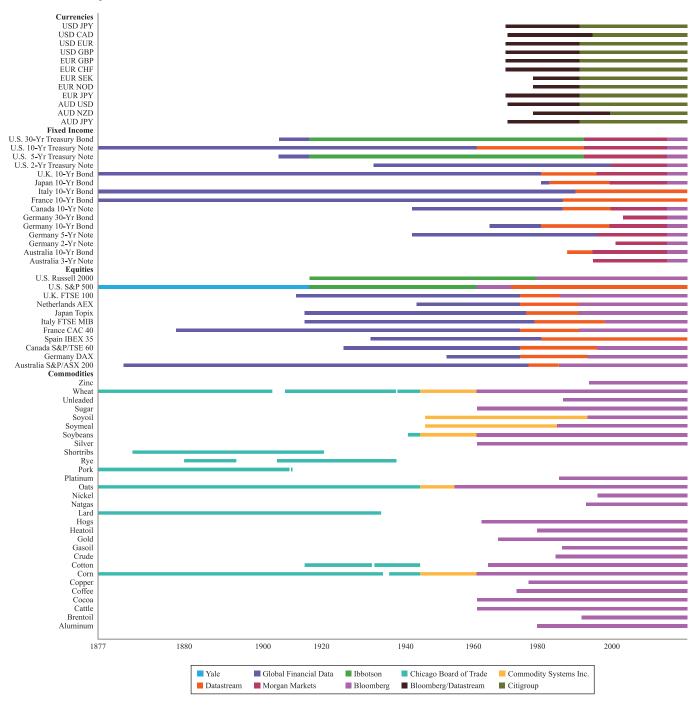
long bond. Futures returns are obtained from Morgan Markets and Bloomberg. We use country-level cash bond returns from Datastream, Ibbotson, and Global Financial Data (GFD) prior to the availability of futures returns. We scale monthly returns from GFD and Ibbotson to a constant duration of 4 years, assuming a duration of 2 years for the U.S. 2-year note, 4 years for the U.S. 5-year note and German REX Index, 20 years for the U.S. long bond, and 7 years for all other bonds.

**Currencies.** The universe of currency forwards covers the following 10 currencies: Australian dollar, Canadian dollar, German mark spliced with the euro, Japanese yen, New Zealand dollar, Norwegian krone, Swedish krona, Swiss franc, British pound, and U.S. dollar. We use spot and forward interest rates from Citigroup to calculate currency returns going back to 1989 for all the currencies except for CAD and NZD, which go back to 1992 and 1996. To calculate returns prior to that, we use spot exchange rates from Datastream and LIBOR short rates from Bloomberg.

**Commodities.** We use a dataset of 29 different commodity futures that is significantly longer than those previously used in the literature. Where available, we use futures price data from Bloomberg. For periods before Bloomberg data is available, we use futures prices from Commodity Systems Inc. and a dataset constructed from the historical records of the Chicago Board of Trade. In particular, the data from 1877 to 1951 was manually transcribed from the Annual Report of the Trade and Commerce of the Chicago Board of Trade (CBOT). To ensure accuracy, we had two independent data vendors transcribe the same dataset, and their transcriptions were cross-verified to be mutually consistent. We note that opening and closing prices were not recorded in the early part of the sample, so we use the average of high and low prices before closing prices are available. Finally,

# EXHIBIT A1

## Data Sources by Market and Time Period



the roll schedule seeks to hold one of the most liquid futures contracts across maturities. For example, each month in the hand-collected data, we hold the nearest of the contracts whose delivery month is at least two months away.

# APPENDIX B

# SIMULATION OF FEES AND TRANSACTION COSTS

To calculate net-of-fee returns for the time-series momentum strategy, we subtracted a 2% annual management fee and a 20% performance fee from the gross-of-fee returns to the strategy. The performance fee is calculated and accrued on a monthly basis but is subject to an annual highwater mark. In other words, a performance fee is subtracted from the gross returns in a given year only if the fund returns are large enough that the fund's end-of-year NAV exceeds every previous end-of-year NAV.

Exhibit B1 reports the transaction costs used to simulate the net returns of the strategy. These costs are based on proprietary estimates, made in 2012, of the average transaction costs for each of the four asset classes, including market impact and commissions. Further, the transaction costs are assumed to be twice as high from 1993 to 2002 and six times as high from 1880 to 1992, based on Jones [2002]. We note

# **E** X H I B I T **B** 1 Simulated Transaction Costs

Asset Class	Time Period	One-Way Transaction Costs (as a % of notional traded)
Equities	1880–1992	0.34%
	1993-2002	0.11%
	2003-2016	0.06%
Bonds	1880-1992	0.06%
	1993-2002	0.02%
	2003-2016	0.01%
Commodities	1880-1992	0.58%
	1993-2002	0.19%
	2003-2016	0.10%
Currencies	1880-1992	0.18%
	1993-2002	0.06%
	2003-2016	0.03%

Note: This exhibit shows the assumed transaction costs for the time period 2003–2016. The transaction costs are assumed to be twice as high from 1993 to 2002 and six times as high from 1880 to 1992, based on Jones [2002].

that the transaction costs are estimated with a significant amount of uncertainty and do not include potential other costs, such as the costs of rolling futures contracts.

#### **ENDNOTES**

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<sup>1</sup>Ricardo's trading rules are discussed by Grant [1838] and the quote attributed to Livermore is from Lefèvre [1923].

<sup>2</sup>The original work on trend-following investing and hedge funds was due to Fung and Hsieh [1997, 2001]. We follow the time-series momentum methodology of Moskowitz et al. [2012]. Research on trends also includes Cutler et al. [1991], Silber [1994], Erb and Harvey [2006], Menkhoff et al. [2012], Baltas and Kosowski [2013, 2015], and Georgopoulou and Wang [2017]. The original evidence on cross-sectional momentum (a strategy closely related to time-series momentum based on a security's performance relative to its peers) is due to Jegadeesh and Titman [1993] and Asness [1994].

<sup>3</sup>See Fung and Hsieh [2001] and Hurst et al. [2013].

<sup>4</sup>Levine and Pedersen [2016] show that time-series momentum in its most general form can capture movingaverage crossover signals and all other linear trend filters.

<sup>5</sup>See also Greyserman and Kaminski [2014], who consider a very long trend-following strategy based on spot prices. Although returns computed based on spot prices are not implementable (because they do not include the effects of the futures "roll down," e.g., even if spot prices exhibit trends, trend-following investing in futures would not be profitable if the futures prices anticipate the trend, on average), our actual futures data allow us to construct a more realistic version of the strategy. Our century of evidence for time-series momentum also complements the evidence that cross-sectional momentum has delivered positive returns in individual equities back to 1866 (Chabot et al. [2009]) and has worked across asset classes (Asness et al. [2013]).

<sup>6</sup>Although we have attempted to create as realistic a simulation as possible, we are not claiming that this strategy as described would have been implementable back in the 1880s. Modern day financing markets didn't exist then, nor did equity index and bond futures markets simulated in this study. The commodities data throughout are based on traded commodities futures prices and are therefore the most realistic, and by the 1980s, most of the returns are based on futures prices. The main point of the study is to show that markets have exhibited statistically significant trends for well over a century.

<sup>7</sup>We use a simple covariance matrix estimated using rolling three-year (equally weighted) monthly returns in the portfolio volatility scaling process.

<sup>8</sup>Although a 2/20 fee structure has been commonplace in the industry, some managers charged higher management and performance fees in earlier time periods. On the other hand, there are also managers that charge lower fees for the strategy today.

<sup>9</sup>Barberis et al. [1998], Daniel et al. [1998], De Long et al. [1990], Hong and Stein [1999], and Frazzini [2006] discuss a number of behavioral tendencies that lead to the existence of price trends.

<sup>10</sup>The 60/40 portfolio has 60% of the portfolio invested in the U.S. equity market and 40% invested in U.S. 10-year government bonds. The portfolio is rebalanced to the 60/40 weights at the end of each month, and no fees or transaction costs are subtracted from the portfolio returns.

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